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On the flexibility of the structural framework of cubic LAMOX compounds, in relationship with their anionic conduction properties

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Abstract

A mathematical analysis of the cubic crystal structure of fast oxide-ion conductor β - $\text{La}_2\text{Mo}_2\text{O}_9$ (and derived members of the LAMOX family) shows that its cationic sublattice can behave as a semi-rigid framework. Tilt/rotation of rigid $[\text{O}1\text{La}_3\text{Mo}]$ anti-tetrahedral units about their 3-fold axis can open up tunnels in the cationic framework, therefore favoring the mobility of O2 and O3 oxide ions located in these tunnels, as confirmed by molecular dynamics simulations. Such a process is likely to assist the anionic transport and explain the postulated transition from Arrhenius-type to VTF(Vogel-Tammann-Fulcher)-type behavior propounded to account for the peculiar conductivity curvature observed at high temperature in all the cubic LAMOX compounds. It also clarifies the correlated extra cell volume expansion observed at the same temperature in all these materials.

Introduction

Many ionic conductors are known to exhibit an order–disorder-type phase transition toward a highly conducting high-temperature phase. It is the case¹ of fast oxide-ion conductor $\text{La}_2\text{Mo}_2\text{O}_9$, whose conductivity above the α/β phase transition (at 580 °C) is about 5 times larger than that of yttrium-stabilized zirconia YSZ8%. Most cationic substitutions, leading to the so-called LAMOX family,² stabilize at room temperature the cubic β phase. The conductivity curves of these cubic phases exhibit the conventional Arrhenius-type behavior at low temperature, but deviate from it at higher temperature (generally above ca. 400 °C), with first an increase and then a leveling off of conductivity. Such an increase, which cannot originate from an increase of the carrier concentration alone,³ has been interpreted as resulting from a transition toward a high-temperature Vogel–Tammann–Fulcher (VTF) regime.⁴

Arrhenius and VTF models are prototypes for activated and assisted transport mechanisms, respectively. The former

(Arrhenius) depicts thermally activated ionic motion in solids, whereas the latter (VTF) is used to model diffusion of highly mobile ionic species, whose migration is assisted by the motion (in polymers⁵ or salt–polymer complexes, above their glass transition) or libration (in ceramics⁶) of the counterionic matrix. In ceramics the semirigid structural framework, acting as a template for mobile ions, remains solid but its rigid constitutive parts are able to tilt and rotate with respect to each other, thus opening up migration pathways and favoring diffusion. Such a process has been advanced to explain the high-temperature ionic motion of LLTO lithium-ion conductors, where the octahedral tilting/rotation around perovskite cages is thought to favor lithium diffusion from cage to cage through the opening/closing of the intercage bottleneck.⁶ In salt–polymer complexes, the VTF regime is interpreted as originating from the natural thermal expansion, which, above a critical temperature T_0 , results in an excess free volume redistributable without any enthalpic contribution.⁷ On another hand, when oxide glasses with ionic conducting properties are modified by the addition of metal–halide salts, it has been shown⁸ that the resulting increase in ionic conductivity scales perfectly (through a cubic power law)

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with the volume expansion generated by the doping. Correlations between ionic conduction and thermal (or chemical) expansion are well-known in oxide ion conductors. Some alternative explanations to free volume have been advanced to explain them, such as the dependence of both conduction and expansion on oxygen vacancy concentration, or the decreasing interaction between ions when the crystal expands (see for instance refs 9 and 10 and references therein). Among the studies focusing more specifically on free volume, depending on the structural type, correlations with ionic conduction have either been clearly evidenced (fluorite¹¹ or brownmillerite¹² types) or shown to be partly counterbalanced by conflicting effects (perovskite^{13,14} or brownmillerite¹⁵ types).

The purpose of this paper is to try to evidence such type of correlations between oxide-ion conduction and thermal expansion in the LAMOX family, and to interpret it in terms of the flexibility of its structural framework.

Experimental Section

Synthesis. Powder samples were prepared by conventional solid-state reaction of intimate mixtures of elementary oxides or carbonates. A preheating of several hours at 500 °C was applied for pre-reaction in order to avoid molybdenum oxide sublimation. One or several firings were performed at high temperature (generally between 900 and 1200 °C depending on composition,^{2,16} with intermediate grindings) until a pure phase is obtained. Pellets with high relative density (>95%) were obtained from ball-milled powders (FRITSCH planetary micromill pulverizette apparatus, with 900 mg of sample in agate vials together with six 10 mm diameter agate balls, in ethanol; 4 alternations of 15 min milling sequences at 700 rpm, with a 15 min pause in between). After mixing with an organic bending agent, dried powders were first shaped in a uniaxial press (~5 mm diameter and 3–5 mm thickness) and then pellets were isostatically pressed at 500 MPa in a Top Industrie room-temperature apparatus. The optimal sintering conditions were determined by dilatometry (see below).

X-ray Diffraction. X-ray powder thermodiffractograms were recorded in air from RT to 1060 °C on a θ/θ Bragg–Brentano Philips X’pert MPD PRO diffractometer (Cu $K\alpha_{1+2}$ radiations) equipped with the X’celerator detector and an Anton Paar HTK1200 high-temperature heating chamber. Diffractograms were collected at each temperature for 184 min in the [15–130°] scattering angle range, with a 0.0167° step (heating rate 10 °C/min between each thermal step, with 20 min temperature stabilization before recording). Crystal cell parameters were determined by full pattern matching refinement of the powder XRD patterns in space group $P2_13$ using the Fullprof program.¹⁷

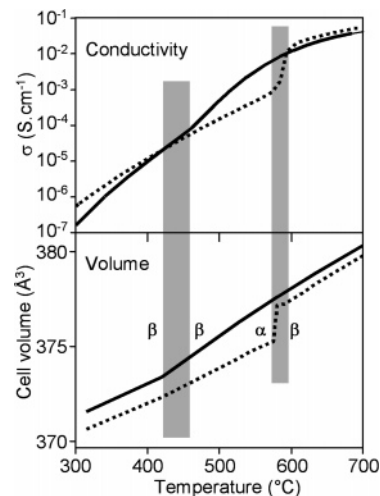


Figure 1. Comparison between measured conductivity increase (top) and measured volumic expansion (bottom) as a function of temperature for $\text{La}_2\text{Mo}_2\text{O}_9$ (dotted lines) and $\text{La}_{1.9}\text{Sr}_{0.1}\text{Mo}_2\text{O}_{8.95}$ (full lines). The gray vertical bars indicate the monoclinic/cubic α/β phase transition in $\text{La}_2\text{Mo}_2\text{O}_9$ at high temperature and the postulated Arrhenius/VTF transition in cubic $\text{La}_{1.9}\text{Sr}_{0.1}\text{Mo}_2\text{O}_{8.95}$ at lower temperature.

Dilatometry. For dilatometric measurements, a vertical SET-ARAM TMA Setsys Evolution 16 dilatometer was used. Linear thermal expansion coefficients were measured on sintered pellets in a 20 mL/min air flow from RT to 1000 °C (5 °C/min heating rate).

Conductivity Measurements. Complex impedance measurements were performed on dense pellets, with thin platinum films (deposited by magnetron sputtering on both flat faces) as electrodes. The impedance spectra were recorded over the 32 MHz to 0.1 Hz frequency range (signal amplitude 50 mV) in dry air flow at high temperature using a Solartron SI 1260 frequency response analyzer combined with the Dielectric Interface (Solartron 1296). A 35 min thermalization time was applied before each measurement.

Molecular Dynamics. A series of molecular dynamics (MD) simulations were performed in order to test the effect of anti-tetrahedra rotation on oxygen mobility. The pair-potential U_{ij} used in this study was the Busing approximation of Born–Mayer–Huggins form

$$U(r_{ij}) = \frac{z_i z_j}{r_{ij}} + f_0 (b_i + b_j) \exp\left(\frac{a_i + a_j - r}{b_i + b_j}\right) - \frac{c_i c_j}{r^6}$$

where r_{ij} is the distance between ions, z_i the effective valence of ion i , f_0 a constant equal to $6.947 \times 10^{-19} \text{ J } \text{Å}^{-1}$, c_i and c_j the parameters of the molecular force term, and a_i and b_i the repulsion term parameters. A list of the parameters used for the current simulation can be found in Table 1.

Conductivity and Crystal Cell Volume Anomalies in the LAMOX Family

A correlation between conductivity increase and volume expansion obviously exists in $\text{La}_2\text{Mo}_2\text{O}_9$ (see Figure 1, experimental data) since the α/β phase transition is accompanied by both an increase of anionic conductivity of about 1 order of magnitude¹ and a cell volume expansion of ca. 0.5%.¹⁸ In the cubic members of the LAMOX family, of course no such abrupt change in cell volume is observed

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since no symmetry change occurs in the whole temperature range. However, a change in the thermal expansion coefficient of several cubic members of the LAMOX family (namely, V-, W-, and Bi-substituted compounds) above ca. 650 K has already been observed.¹⁹ It was associated by the authors to either a disordering of oxygen sublattice or possibly a minor oxygen loss indicated by increasing of n-type electronic transference number when the temperature increases. We think the second alternative is most unlikely, specially in the case of W-substituted compounds which are known to be more stable to reducibility than $\text{La}_2\text{Mo}_2\text{O}_9$,²⁰ this last compound having a very low electronic transference number at 750 °C in air (around 10^{-3} , from ref 4). Our interpretation is that such a change in volume expansion should rather be correlated with a change in oxygen transport mechanism from thermally activated (Arrhenius) at low T to thermally assisted (VTF) at high T , in other words with a transition from a static to a dynamic disorder of oxide ions. As a matter of fact, such an increase in cell volume occurs at the same temperature as the conductivity increase (which can also be seen in oxygen tracer diffusion measurements²¹). This is illustrated in Figure 1 with the experimental conductivity and volumetric curves of another cubic member of the LAMOX family, $\text{La}_{1.9}\text{Sr}_{0.1}\text{Mo}_2\text{O}_{8.95}$.

The previous assumption is in qualitative agreement with the correlation established in the earlier study on modified oxide glasses.⁸ The advantage of a crystalline over an amorphous matrix is that the known crystal host framework can be directly analyzed in terms of the ability of its atomic arrangement to accommodate for such an extra volume expansion relative to its own natural thermal expansion. The next section is devoted to such an analysis.

Flexibility of the $\beta\text{-La}_2\text{Mo}_2\text{O}_9$ Cationic Framework

Defining the Most Appropriate Reference Frame.

The conventional manner to represent an oxide structure, featuring the ligand coordination environment of cations, is not the most appropriate way to describe the structural arrangement of $\beta\text{-La}_2\text{Mo}_2\text{O}_9$. This is due to the fact that the partial occupancy of most oxide ions sites does not allow an easy or convenient polyhedral representation, especially when our understanding of transport properties requests a differentiation between those oxide ions which are likely to migrate and those which belong to the host framework.

Recently, we have proposed a new kind of description of the $\beta\text{-La}_2\text{Mo}_2\text{O}_9$ structural arrangement based on anti-polyhedra.¹⁶ As a matter of fact, fully occupied sites in the

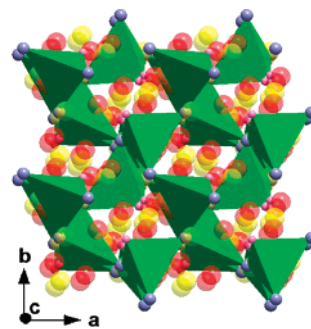


Figure 2. Representation of the $\beta\text{-La}_2\text{Mo}_2\text{O}_9$ structural type in terms of a [OLaMo] framework built up from La corner-sharing [O1La₃Mo] anti-tetrahedral units (green), with O2 and O3 oxide ions sites imbedded in its tunnels.¹⁶ Pink spheres = Mo⁶⁺ or substitute, blue spheres = La³⁺ or substitute, yellow and red transparent spheres = O2 and O3 oxide ion sites, respectively.

structure (La, Mo, and O1, in 4a positions of space group $P2_13$) form tetrahedral units around the O1 sites, hereafter called [O1La₃Mo] anti-tetrahedra. These anti-tetrahedral units are supposed to be the most stable part of the structure and O1 the less mobile oxide ion since it is surrounded by four cations. In comparison, O2 and O3 are surrounded by three cations only²² and are therefore less trapped than O1. Moreover, O2 and O3 sites are partially occupied and have larger and more anisotropic Debye–Waller thermal factor than O1.¹⁸ Each [O1La₃Mo] anti-tetrahedron shares its three La vertexes with two other anti-tetrahedra to form a 3D framework with formulation [OLaMo]. Such a framework delineates tunnels in which are located partially occupied O2 and O3 sites on 12b positions (see Figure 2). Incidentally, these two O2 and O3 sites are thought to be occupied by charge carriers,²¹ thus providing an interesting and suggestive connection with transport properties. In this new description, the molybdate formula becomes [OLaMo]₂O₇□ with seven oxide ions (and a vacancy, according to the LPS concept²³) inside the voids of the [OLaMo] framework.

We thus adopt, with this kind of representation, a symmetrical approach²⁴ to that commonly used in describing the structure/properties relationships in cation conductors: indeed, cationic anti-polyhedra for anionic conductors are equivalent to (or play the same role as) anionic polyhedra for cationic conductors. For instance, migrating oxide anions are likely to move, inside the [OLa₃Mo] anti-tetrahedra-based framework in $\beta\text{-La}_2\text{Mo}_2\text{O}_9$, the same way as lithium cations do inside the [TiO₆] octahedral-based framework in the LLTO perovskite structure.

Therefore, what we want to check now is whether anti-tetrahedra in cubic LAMOX can easily tilt and rotate the same way as octahedra can do in the perovskite structure.

Anti-tetrahedral [O1LaMo] Host Matrix as a Semirigid Framework. As reported in the Introduction, lithium migration above room temperature in LLTO perovskites is thought to be assisted from perovskite cage to perovskite cage by octahedra tilting/rotation. In this respect the octahedral framework is considered to be semirigid, with

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rigid octahedral units allowed to rotate around their vertexes. The equivalent of the perovskite rigid octahedral unit in cubic LAMOX is the anti-tetrahedral $[\text{OLa}_3\text{Mo}]$ unit represented in Figure 3, whose geometry in this symmetry is fixed by the three interatomic distances La–La (d_{\parallel}), La–Mo (d_{lm}), and Mo–O1 (d_{mo}). In space group $P2_13$, all three atoms are located in 4a sites on a 3-fold axis (O1 and Mo on the same 3-fold axis), with only one atomic coordinate each ($x = y = z$). Indeed the interatomic distances can be expressed in terms of the atomic positions (hereafter called x_l , x_m , and x_o for La, Mo, and O1, respectively) and of the a cubic cell parameter. The main idea is then to deduce from these relationships the expression of the atomic position parameters x_l , x_m , and x_o as a function of the cell parameter a and of geometrical characteristics of the anti-tetrahedra d_{\parallel} , d_{lm} , and d_{mo} . The core of our approach can be outlined as follows, with $f(\cdot)$, $f'(\cdot)$, $f''(\cdot)$, $g'(\cdot)$, $g''(\cdot)$, $h'(\cdot)$, etc..., representing functions of (\cdot) :

$$d_{\parallel} = g'(a, x_l) \Rightarrow x_l = f'(a, d_{\parallel}) \quad (1)$$

$$d_{\text{lm}} = g''(a, x_l, x_m) \Rightarrow x_m = h''(a, x_l, d_{\text{lm}}) = f''(a, d_{\parallel}, d_{\text{lm}}) \quad (2)$$

$$d_{\text{mo}} = g'''(a, x_m, x_o) \Rightarrow x_o = h'''(a, x_m, d_{\text{mo}}) = f'''(a, d_{\parallel}, d_{\text{lm}}, d_{\text{mo}}) \quad (3)$$

leading finally to

$$(x_l, x_m, x_o) = f(a, d_{\parallel}, d_{\text{lm}}, d_{\text{mo}}) \quad (4)$$

The expressions of d_{\parallel} , d_{lm} , and d_{mo} are quadratic forms of x_l , x_m , and x_o . The atomic coordinates are therefore roots of the corresponding equations that can be successively inserted into the next equation in order to get a global solution to the system, provided that these roots exist in the functional definition ranges (positive discriminant). One ends up with the following set of expressions:

$$x_l = (7 - \sqrt{\Delta_1})/8 \quad (1')$$

with

$$\Delta_1 = 8(d_{\parallel}/a)^2 - 3 \quad (1'')$$

$$x_m = (2 - \sqrt{\Delta_2} - x_l)/3 \quad (2')$$

with

$$\Delta_2 = -8x_l^2 + 14x_l + 3(d_{\text{lm}}/a)^2 - 13/2 \quad (2'')$$

$$x_o = x_m + d_{\text{mo}}/(a\sqrt{3}) \quad (3')$$

Formula (1') is valid, and therefore the cationic arrangement is self-consistent, only if $\Delta_1 \geq 0$, that is, from (1''): $d_{\parallel}/a \geq \sqrt{3/8} \cong 0.61237$. According to (1'), the maximum possible value of x_l is obtained for $\Delta_1 = 0$, that is, $x_l^{\text{max}} = 7/8 = 0.875$.

Formula (2') is more complex since it relates the atomic positions of two different atoms. Of course, it requests that $\Delta_2 \geq 0$ which, through (2''), delimits bounds on interatomic distances and/or lanthanum position. Defining precisely these

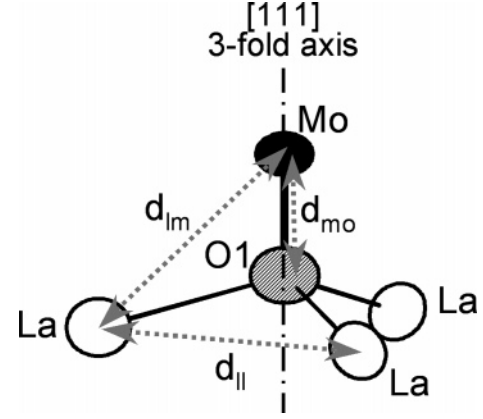


Figure 3. $[\text{O1La}_3\text{Mo}]$ anti-tetrahedral basic units, with the interatomic distances considered in the text.

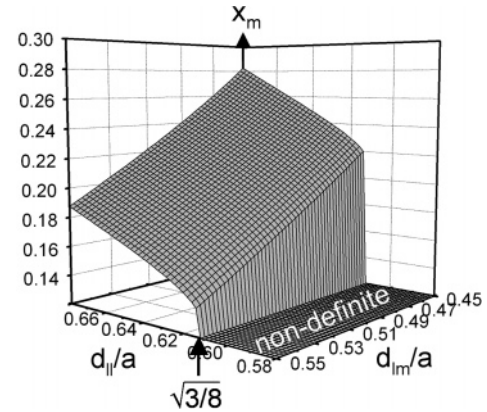


Figure 4. Molybdenum atomic coordinate x_m as a function of d_{\parallel}/a and d_{lm}/a in a semirigid $[\text{OLaMo}]$ framework.

bounds is of little interest here. Just notice that, for the current study range of relevance (see below), Δ_2 is always positive definite. An illustration is given in Figure 4, which shows the evolution of x_m as a function of d_{\parallel}/a and d_{lm}/a (when either the geometry of anti-tetrahedral units or the cell parameter are modified).

Finally, formula (3') is a straightforward relationship which relates the O1 site position to the Mo site position through their interatomic distance.

The interesting point about the current analysis is that, given a reasonable set of La–La, La–Mo, and Mo–O1 interatomic distances and a cubic cell parameter, it is possible to find the La, Mo, and O1 atomic positions which satisfy this set of distances. In other words, given the geometry of a rigid $[\text{O1La}_3\text{Mo}]$ anti-tetrahedral unit, it is possible, for any value of the a cubic cell parameter (smaller than $d_{\parallel}/\sqrt{3/8}$), to find the atomic coordinates which satisfy the anti-tetrahedra geometry (see Figure 5). This is an important result since it shows that the LAMOX anti-framework can be, at least theoretically, flexible enough to accommodate, without any change in symmetry (the above calculations being carried out in the $P2_13$ space group), the tilt/rotation of rigid anti-tetrahedral units and concomitant cell volume change. The anti-framework can thus be folded or unfolded by just closing or opening up the O1–La–O1 interunits angle without modifying the geometry of the anti-tetrahedral units.

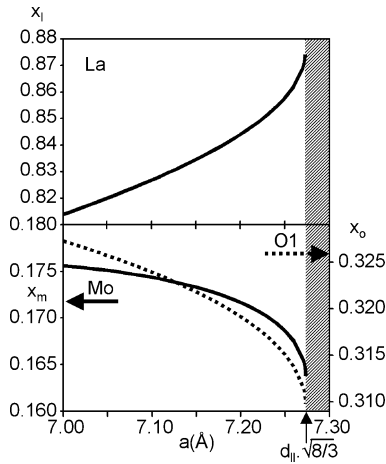


Figure 5. Position of the atoms of rigid [O1La₃Mo] anti-tetrahedral units in the crystal cell as a function of the cubic cell parameter (from interatomic distances measured in β -La₂Mo₂O₉ at 670 °C:¹⁸ $d_{II} = 4.454$ Å, $d_{Im} = 3.703$ Å, $d_{mo} = 1.839$ Å).

Figure 6 shows, from two different standpoints, the unfolding process. Along the tunnels, one can clearly see that the anti-tetrahedra tilting opens up the channels, thus releasing extra free volume for mobile ions. The view along the 3-fold axis (main diagonal axis of the cubic cell) is also interesting because it makes clear the true nature of the anti-tetrahedra movement during the folding/unfolding process: it consists of a rotation around the 3-fold axes ([111] directions) of the structure, passing through the [O1–Mo] axis of the anti-tetrahedra units. The rotation angle δ can be calculated from the (x,y) La atomic coordinates in a hexagonal reference frame, obtained by applying the rhombohedral-to-hexagonal transformation matrix to the La coordinates in cubic reference (see ref 25). It gives a simple relationship between δ and x_l or d_{II}/a :

$$\begin{aligned} \tan(\delta) &= (8x_l - 7)/\sqrt{3} \\ &= -\sqrt{[8(d_{II}/a)^2/3 - 1]} \end{aligned} \quad (5)$$

or a as a function of δ :

$$a = d_{II}/\sqrt{[3(1 + \tan^2(\delta))/8]} \quad (6)$$

In these formulas δ is negative, $\delta = 0$ corresponding to maximal volume expansion (for $x_l = 7/8$ or $d_{II}/a = \sqrt{[3/8]}$). Figure 7 shows the calculated cell parameter evolution when the rotation angle varies, as deduced from formula (6).

4.3. Framework Flexibility and Ionic Conductivity. In an ionic conductor, the free volume is a volume available for ions to move. The larger this volume, the higher the ionic mobility. In the hypothesis of an Arrhenius/VTF type

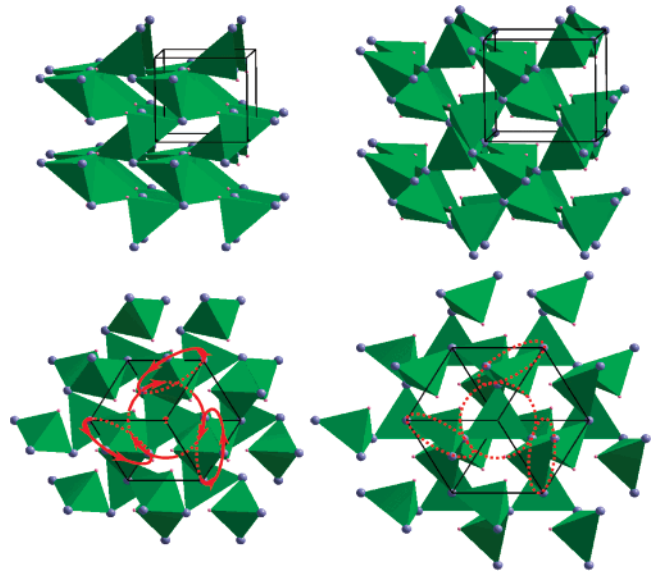


Figure 6. Folded (left, exaggerated) and unfolded (right) anti-framework as viewed along two directions of the β -La₂Mo₂O₉ type structure: along the tunnels parallel to the cubic cell axis (upper) and along the 3-fold axis (lower). The rotation of [O1La₃Mo] anti-tetrahedral units is outlined.

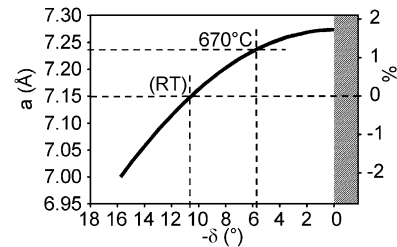


Figure 7. Calculated cubic cell parameter as a function of the δ rotation angle of rigid [O1La₃Mo] anti-tetrahedral units (with imposed geometry $d_{II} = 4.454$ Å, $d_{Im} = 3.703$ Å, $d_{mo} = 1.839$ Å). The dashed lines indicate the cell parameter and rotation angle of β -La₂Mo₂O₉ at 670 °C (from crystal structure data, ref 18) and their approximation in a pseudo-cubic cell at room temperature.

transition, it seems reasonable to think that the increase of mobility in the VTF regime is correlated to an expansion of free volume, and therefore in our case of the crystal cell parameter. Such an expansion and its correlation with the conductivity increase are clearly evidenced in the experimental data displayed in Figure 1. It is also observed in all other cubic members of the LAMOX family (see Figure 8) with more or less magnitude depending on the substituent, which also influences the Arrhenius/VTF transition temperature.³ Two expansion regimes are observed: a regular one at low temperature, with constant expansion coefficient, and an extra expansion at higher temperature, correlated to the appearance of the VTF regime. From the very nature of the VTF mechanism, the host matrix is supposed to assist oxygen migration, and it is likely that the flexibility of the LAMOX framework is at the origin of the observed volume increase, through anti-tetrahedral rotation/vibration. The “empty” volume (cell volume – atomic volume) is relatively large in La₂Mo₂O₉ since it represents about 38% of the cell volume (as compared to 26% in a close packed arrangement). Any additional volume freed up by the anti-tetrahedra rotation is likely to favor the ionic mobility, or to be correlated to it. Figure 9 reports the experimental thermal expansion of the

(25) Hahn, Th., Ed. *International Tables for Crystallography, Vol. A, SpaceGroup Symmetry*, 4th ed.; Kluwer Academic Publishers: Norwell, MA, 1995; p 78. Namely, the

$$\begin{bmatrix} -1/3 & 2/3 & -1/3 \\ -2/3 & 1/3 & 1/3 \\ 1/3 & 1/3 & 1/3 \end{bmatrix}$$

matrix is applied to the $(-1/2 + x_l, 3/2 - x_l, 1 - x_l)$ lanthanum coordinates.

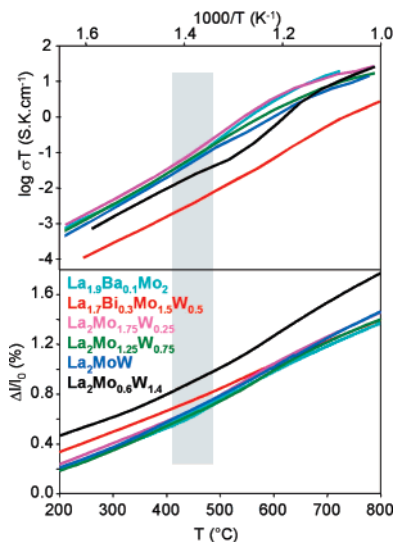


Figure 8. Departure from linearity at high temperature in the thermal expansion (bottom) and the Arrhenius plot of conductivity (top) of a series of LAMOX compounds (whose cationic stoichiometry is indicated). The two temperature scales coincide around $1000/T(K) \sim 1.4$, $T \sim 440$ °C.

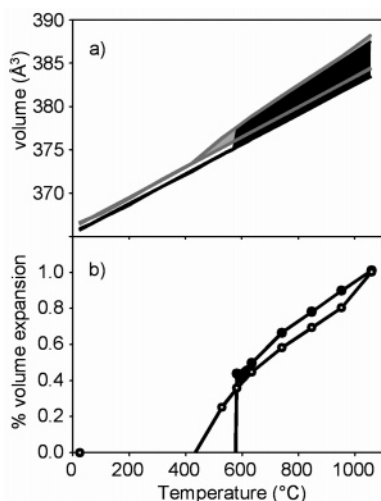


Figure 9. Experimental LAMOX cell volume expansion with temperature: (a) raw data with emphasis on extra expansion relative to regular thermal expansion ($\text{La}_2\text{Mo}_2\text{O}_9$ in black and $\text{La}_{1.9}\text{Sr}_{0.1}\text{Mo}_2\text{O}_{8.95}$ in gray); (b) relative extra volume expansion in excess to regular thermal expansion (black circles for $\text{La}_2\text{Mo}_2\text{O}_9$, open circles for $\text{La}_{1.9}\text{Sr}_{0.1}\text{Mo}_2\text{O}_{8.95}$).

$\text{La}_2\text{Mo}_2\text{O}_9$ and $\text{La}_{1.9}\text{Sr}_{0.1}\text{Mo}_2\text{O}_{8.95}$ cell volumes (a) and the same volume expansion data after linear thermal effects, deduced from low T thermal behavior, are subtracted (b). In both compounds, an extra 0.5–1% volume expansion cannot be accounted for by the regular thermal expansion observed at low temperature. Our proposition is that this additional expansion originates from the rotation of anti-tetrahedral units, at the origin of the high mobility of O2/O3 oxide ions in the anti-framework tunnels. Such an interpretation is illustrated in Figure 10, which combines the experimental data of Figure 1 and our model calculation of Figure 7. A rotation of the order of 1° , over about 500 K, of $[\text{O}1(\text{La},\text{Sr})_3\text{Mo}]$ units around their 3-fold axis would account for the observed extra increase in cell volume.

In the next section, we will try to evidence a correlation between such a volume expansion through anti-tetrahedra

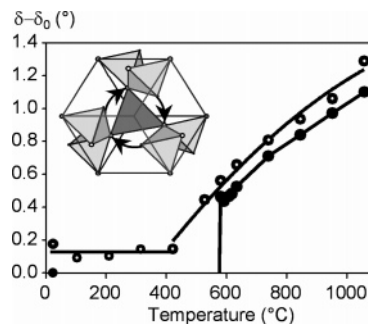


Figure 10. Thermal expansion data of Figure 9 replotted as a function of the δ rotation angle (in insert) deduced from analytical formula (5), for $\text{La}_2\text{Mo}_2\text{O}_9$ (black circles) and $\text{La}_{1.9}\text{Sr}_{0.1}\text{Mo}_2\text{O}_{8.95}$ (open circles).

Table 1. Potential Parameter Set Used for Molecular Dynamics Simulations

ion	parameters			
	z_i	a_i (Å)	b_i (Å)	c_i ($(\text{J } \text{Å}^6 \text{ mol}^{-1})^{1/2}$)
Mo^{6+}	4.05 ^a	0.887	0.0428	0.00
La^{3+}	2.025 ^a	1.410	0.0540	0.00
O^{2-}	-1.35 ^a	1.847 ^a	0.166 ^a	1294 ^a

^a Taken from ref 26.

rotation and an increase of oxide-ion conduction, using molecular dynamics simulations.

Molecular Dynamics Simulations

To check the incidence of such a tilt/rotation of anti-tetrahedra units on the migration of O2 and O3 oxygen sites located in the tunnels of the anti-structure, a series of molecular dynamics simulations were carried out with different rotation angles of these units. The pair-potential function used in this study is given in the Experimental Section. The simulation parameters for O^{2-} ions and effective charge for all ions were taken from ref 26. The parameters for Mo^{6+} and La^{3+} ions were determined so as to minimize atomic displacement from the atomic positions determined on a La_2MoO_6 crystal.²⁷ This set of parameters, as listed in Table 1, has been shown to reproduce accurately the first coordination sphere of La and Mo in $\text{La}_2\text{Mo}_3\text{O}_{12}$,²⁸ $\text{La}_2\text{Mo}_4\text{O}_{15}$,²⁹ and $\beta\text{-La}_2\text{Mo}_2\text{O}_9$ at 943 K.¹⁸ The pair radial distribution functions, involving O2 and O3 oxide ions only, in a 64 cells sample of $\beta\text{-La}_2\text{Mo}_2\text{O}_9$ after relaxation at 943 K (see below) are shown in Figure 11 (for full coordination sphere of cations, add one O1 for Mo^{6+} and three O1 for La^{3+}). They are consistent with the crystal structure.¹⁸

A cubic MD simulation box consisting of $4a \times 4a \times 4a$ crystallographic unit cells was chosen. The d_{11} , d_{1m} , and d_{m0} interatomic distances of $\beta\text{-La}_2\text{Mo}_2\text{O}_9$ at 943 K were taken as reference.¹⁸ A series of rotation angles were chosen, spanned around the value measured in $\beta\text{-La}_2\text{Mo}_2\text{O}_9$ at this temperature ($\delta = -5.85^\circ$). The corresponding crystal cell parameters a and La, Mo, and O₁ atomic coordinates, as

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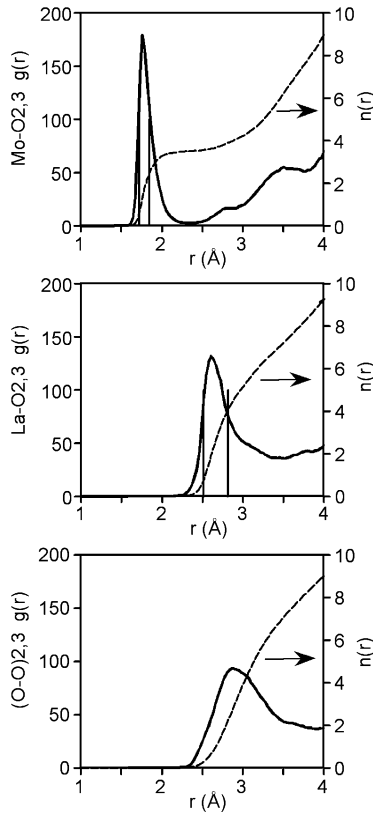


Figure 11. Radial distribution function $g_{ij}(r)$ and coordination number distribution $n_{ij}(r)$ versus the interionic distance r in the cation–anion (Mo–O_{2,3} and La–O_{2,3}) and anion–anion (O_{2,3}–O_{2,3}) pairs, after molecular dynamics relaxation at 943 K. For full cationic coordination numbers, one and three O1 extra neighbors should be added to Mo and La polyhedra, respectively. Vertical lines correspond to the crystal structure interatomic distances (from ref 18).

Table 2. Crystallographic Cell Parameter a and Corresponding Atom Coordinates (Calculated from Formulas (1'), (2'), (3'), and (6)) Used in the Molecular Dynamics Simulations

δ (deg)	a (Å)	$x(\text{La})$	$x(\text{Mo})$	$x(\text{O}_1)$
0	7.273352	0.875000	0.163496	0.309474
–5	7.245674	0.856058	0.169002	0.315537
–5.85	7.23511 ^a	0.8528 ^a	0.1697 ^a	0.3165 ^a
–7.5	7.211127	0.846496	0.171172	0.318409
–10	7.162853	0.836824	0.172958	0.321188
–15	7.025518	0.816987	0.175372	0.326500
–20	6.834715	0.796198	0.176189	0.331536

^a From ref 18.

deduced from formulas (6), (1'), (2'), and (3'), respectively, were kept fixed during each simulation run (see Table 2). The O₂ and O₃ oxygen ions were chosen randomly to match the occupation ratio, but a constraint was used to exclude small O–O distances. However, short O–O (i.e., 1.2–1.7 Å) could not be avoided. The box thus contained 256 Mo, 256 La, 256 O₁, 600 O₂, and 296 O₃ ions, periodic boundary conditions were employed, and the time step was equal to 2×10^{-15} s. The initial velocity of O₂ and O₃ ions were sampled from a Maxwell–Boltzmann distribution at the temperature specified for the simulation, with Mo, La, and O₁ being kept fixed. The system was relaxed at 943 K for 25000 time steps and then heated at 1500 K in one step and then relaxed again for 80000 more time steps. The 1500 K temperature was selected instead of 943 K in order to obtain accurate displacement.

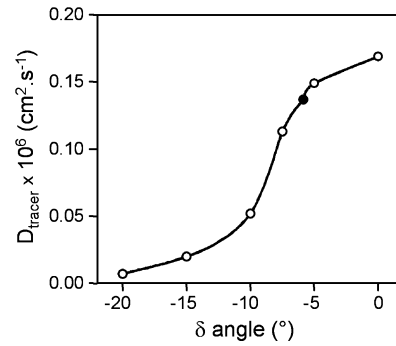


Figure 12. O₂+O₃ diffusion coefficient at various anti-tetrahedra rotation angles δ , from molecular dynamics simulations at 1500 K. The reported values correspond to the average over 10 runs of 160 ps duration each. The solid dot corresponds to the structural framework arrangement of β -La₂Mo₂O₉ at 943 K.¹⁸

The bulk oxygen tracer diffusion coefficient D_{tracer} was computed via the time-dependent mean square displacement³⁰ denoted by $s^2(t)$:

$$s^2(t) = \frac{1}{N} \sum_{n=1}^N \langle [\bar{r}_n(t_0 + t) - \bar{r}_n(t_0)]^2 \rangle = C + 6D(t) \times t$$

where $\bar{r}_n(t)$ is the position vector of the n th oxygen ion (O₂ or O₃) at the time t ; C is a constant. D_{tracer} is taken as the asymptotic value of $D(t)$ with a time calculation of 160 ps (i.e., 80000 time steps).

The dependence of the diffusion coefficient on the anti-tetrahedra tilt/rotation angle is plotted in Figure 12. A significant increase, of about 1 order of magnitude in a few degrees of rotation, is observed between -10° and -5° , that is to say just below the tilting angle measured at 670 °C in β -La₂Mo₂O₉ ($\delta = -5.85^\circ$). These simulations therefore show that an opening up of the anti-structure tunnels through anti-tetrahedra rotation would be responsible for an increase in the O₂ and O₃ oxygen mobility, thus confirming the self-consistency of our model.

We also attempted to observe individual oxygen jumps during the simulation. Since trajectory analysis requires long displacements, we had to use a smaller box, i.e., a $3a \times 3a \times 3a$ crystallographic unit cell (108 Mo, 108 La, 108 O₁, 253 O₂, and 125 O₃ ions) in order to reduce time calculations. Figure 13 shows 3D plots of the trajectory of some O₂ or O₃ oxygen recorded at 1500 K in the most favorable geometry ($\delta = 0^\circ$), as well as the related atomic coordinates as a function of time. One clearly sees discrete jumps, which could be responsible for the oxygen diffusion in La₂Mo₂O₉. The mean jump length involving O₂/O₃ ions is 2.8 Å, close to the mean O–O distance obtained on the simulated radial distribution function, and to the nearest oxide ion neighbors distance measured from the short-range-order modulation of the neutron diffraction background.^{31,16} Note also that the jumps detected on O₂ and O₃ oxide ions #699 and #402 are time-correlated at around 330 ps, with ion O₂ occupying after its jump the previous position of ion O₃ just before its jump.

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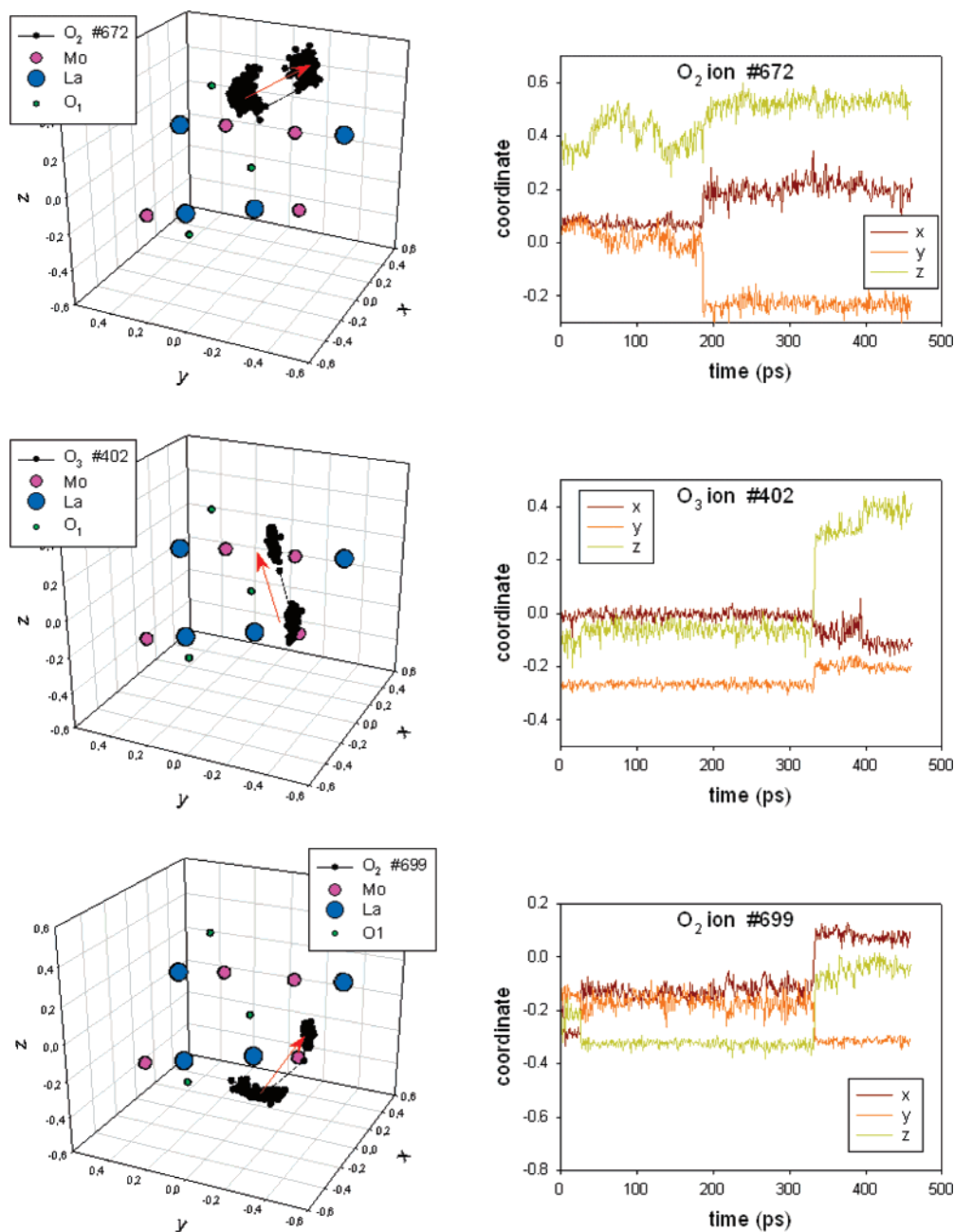


Figure 13. From the molecular dynamics simulation of a sample with fully opened framework ($\delta = 0^\circ$) at 1500 K, the trajectory and atomic coordinates versus time of some oxide ions indexed as #402 (O₃), #672 (O₂), and #699 (O₃). NB: O₂ and O₃ are labeled according to their original positioning, but subsequent migrations prevent any real differentiated allocation (localizations in black in the 3D trajectory charts).

Discussion

The flexibility of polyhedral networks, and in particular tetrahedral networks, has been extensively studied by various techniques, including simulation and geometrical analysis (see for instance refs 32 and references therein). The basic concept of all these studies is that of the “rigid-unit mode” (abbreviated as RUM)³³ model, which assumes that there exist, in these networks, rigid polyhedral units whose low-

energy vibration modes ensure structural flexibility. The most famous and studied applications of such a concept concern silicates or aluminosilicates (phosphates) with corner-sharing rigid (Si,Al,P)O₄ tetrahedra. As a matter of fact, in SiO_{4/2} networks, the energy cost for a distortion of the 2-fold coordination environment of oxide ions is probably smaller than that for a distortion of the 4-fold coordination polyhedra of silicon.

Our approach in this paper is to invert the pattern and use OM₄ anti-tetrahedral units as the building rigid blocks of the RUM model. This is a risky assumption since the

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coordination sphere of cations is usually larger, in term of ligand numbers, than the coordination sphere of anions, so that a distortion of the latter would remain less energy costly than a distortion of the former, as in the previous silicate cases. Indeed, if one takes into account partial occupancies of oxide ions, the average coordination numbers of Mo^{6+} and La^{3+} in $\beta\text{-La}_2\text{Mo}_2\text{O}_9$ are 4.5 and 10, respectively,¹⁸ as compared to 4 for O1 anion. However, as mentioned earlier and due to the fast oxide-ion properties of this molybdate, O2 and O3 are rather mobile ligands around molybdenum and lanthanum, themselves elements which tolerate a high flexibility in their coordination spheres. If one assumes that fully occupied O1 is the most tightly bound ligand, therefore creating the most rigid links, Mo^{6+} and La^{3+} have only one and three such rigid bounds in their surroundings, respectively,¹⁸ whereas O1 has four. And on average, one therefore ends up with twice more strong bounds around O1 than around cations, a reversed situation when compared to that of silicates.

Even if at first sight it might appear astonishing that the flexibility of the $\beta\text{-La}_2\text{Mo}_2\text{O}_9$ framework could rely upon the displacement of such heavy atoms as La or Mo, a similar case has already been referred to in the literature. In zirconium tungstate ZrW_2O_8 , a compound known for its negative thermal expansion properties, it has been shown that the Zr–O–W linkage remains rather stiff with temperature (with no important static³⁴ or dynamic³⁵ opening up of the interatomic angle) and that the low-energy vibrational modes involve heavy Zr and W atoms. That a comparable type of low-energy mode involving rigid La–O–(Mo,B) links could occur in $\text{La}_2(\text{Mo,B})_2\text{O}_9$ is therefore not so surprising.

On the other hand, even with a certain stiffness of La–O1–(Mo,B) links in anti-tetrahedral units, the assumption that these units keep exactly the same geometry upon heating, even with some isotropic thermal expansion, might not be very realistic. As a matter of fact, we have already shown that anti-tetrahedra can distort upon chemical substitution,³ and it would not be so surprising if chemical bonds had different thermal expansion depending on the nature of the involved cation. Such additional effect, not taken into account in our model, could for instance be at the origin of differences in oxygen tracer diffusion coefficients, which appear to be somewhat smaller in our MD simulations than the ones measured on real samples.²¹ Nevertheless, we think that our proposition, even crude as it is, gives a plausible explanation for the main structural/transport anomalies observed in these compounds and should be tested further.

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It is also probable that the observed lattice expansion does not result from a smooth regular opening of the anti-structural framework only, but that it takes place through a libration process with dynamical breathing of the framework. Such a libration would thus assist oxygen migration, in somewhat the same way as in LLTO perovskites, octahedral librations (which allow for the opening/closing of the inter-cage bottleneck), do for lithium migration.

Conclusion

In this paper, we have studied through a mathematical analysis the ability of the $\beta\text{-La}_2\text{Mo}_2\text{O}_9$ cationic sublattice to distort as a semirigid framework of tilting $[\text{OLa}_3\text{Mo}]$ anti-tetrahedral units. It is theoretically possible in a surprisingly large rotational domain (although atomic repulsion certainly limits it within a narrower range). It has been proposed that the extra volume expansion, observed at the postulated Arrhenius/VTF transition, originates from such a tilting mechanism. This hypothesis has been tested using molecular dynamics simulations, which confirmed that such an opening of anti-tetrahedral framework induces an increase of oxide-ion diffusion in the tunnels of the structure. However, the magnitude of the structural distortion is expected to be very small (around 1° over a 500 K range³⁶), which should make it difficult to be detected, specially as it is most certainly correlated to a dynamic redistribution of O2/O3 ion sites. Further studies using different techniques will be devoted to its detection.

Finally, the current study has shown that the way we are looking at structures and describing them is not neutral since it has an incidence on our understanding of their properties. As a matter of fact, this analysis would not have been possible if an alternative description of the structural arrangement of $\beta\text{-La}_2\text{Mo}_2\text{O}_9$ had not been striven for, inspired by the pioneering work by O’Keeffe and Hyde 20 years ago.²⁴

Acknowledgment. B. Boulard is grateful to J. Kieffer and C.A. Angell (Arizona State University) for providing the Molecular Dynamics program.

(36) Although comparable in magnitude, the first-order transition in $\text{La}_2\text{Mo}_2\text{O}_9$ cannot be explained the same way since it results from an order–disorder type transition between phases with different symmetries.^{18,37} The physical origin of the transition is however comparable to that observed in cubic LAMOX compounds, except that in this last case the random cationic distribution prevents any oxide-ion/vacancy ordering (and therefore any symmetry breaking).

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